



Engineering Sciences and Mathematics doctoral school
PhD field: Mechanical Engineering

PhD THESIS – ABSTRACT

STUDIES AND RESEARCHES REGARDING THE BIOMECHANICS OF THE FOOT AND THE AXIAL DEVIATIONS WITHIN IT

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SUMMARY



The PhD thesis entitled "Studies and researches regarding the biomechanics of the foot and the axial deviations within it" includes:

- 9 Chapters;
- 281 figures;
- 25 tables;
- 111 references.

The studies and researches related to this thesis were carried out over three years and the paper approaches from a biomechanical point of view the axial deviations conditions of the foot, specifically the Hallux Valgus pathology.

KEY WORDS: foot surgery, gait biomechanics, Skeleton systems method, constructive-anatomical entity, real bone structure, parameterized assembly, CAD, CAE, finite element analysis, MT1 open wedge osteotomy, CORA (Center of Rotation of Angulation), geometric planning optimization, CNC program, Haas ST-15Y.

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Introduction

This PhD thesis is the outcome of the theoretical and experimental researches carried out over three years, the main topic is an interdisciplinary one, and the field in which it focuses being the biomedical or medical engineering.

The reasons why we decided to approach such a topic will be presented as follows:

The first reason is that this field of medical engineering or bioengineering requires in-depth engineering approaches. The human body as a whole is of a very high complexity, having to perform varied and elaborate functions and, unfortunately, can also be affected by various pathologies. In order to treat these pathologies, it is necessary to accurately reproduce these natural functions, which is complex task.

The anatomical site covered is that of the human foot, focusing on the axial deviations that can occur in this area. The study of these pathologies of the foot requires in-depth engineering approaches, based on methods in the engineering field. A conclusive example of this is the fact that in current treatment strategies, to achieve the precision required for interventions, it is necessary to use various geometric and dimensional references, especially when optimising a process.

The second reason why we decided to study the biomedical theme is due to the fact that the results of the research carried out could have a favourable social impact.

Today's society often imposes certain wardrobe standards and often, for the sake of inclusion in a certain group or simply because we want to be in step with fashion, we are willing to make certain compromises, such as wearing an uncomfortable or tight type of footwear. Wearing this type of footwear or high heels favours the development of Hallux Valgus type axial deviations or can aggravate existing ones, which is why around 25% of men and 58% of women (30% of whom are under 25) are affected by this pathological condition.

The third reason for approaching this topic is the goal of increasing the precision of the surgical procedure. Thus, the study of the biomechanics of the foot and related pathologies using CAD-CAE methods, the virtual simulation of surgical procedures, the establishment of reference systems, well-defined dimensional and geometric references make the geometric planning of surgery clearer and safer.

The results of the thesis can be a guide to developing sound treatment strategies, planning operations, using the best methods for preserving corrected positions and determining optimal post-operative recovery possibilities.

CAD modelling of the osteoarticular assembly of the foot was carried out taking into account the real bone structure and aiming at a complete parameterisation of it, for a good

control of basic and associated movements, gait simulation and intermediate phases, as well as easy generation of related pathological conditions.

The correction method that we decided to investigate further was the proximal opening-wedge osteotomy of the first metatarsal, a relatively recent, viable method that shows satisfying results. The main aspect studied was the optimization of this type of surgery in terms of osteotomy positioning, relative to the bone surfaces, by carrying out both CAD-CAE studies and relevant experimental research.

From our point of view, this scientific approach is an important and interesting one in the field of optimizing surgical interventions performed at the osteoarticular foot level. Also, based on this study, other research directions can be derived, such as the study of the biomechanics of the foot in post-operative form, the design of specialized guiding devices to ensure the optimal position of osteotomes or other variants of devices to preserve the positions resulting from angulation correction.

The objectives of the PhD thesis

Based on the interdisciplinary approach of the thesis, the process of establishing the topic has been very thorough, due to the fact that there are many subjects on which studies of interest can be developed, such as the study of non-invasive technologies or devices for the correction of axial deviations of the foot - specialized orthoses, the development of customized prostheses executed by additive manufacturing, the optimization of osteotomies layouts according to the behaviours of post-operative configurations, etc.

The main aim of this PhD thesis is to carry out in-depth biomechanical studies of the existing bone structures of the foot in the orthostatic position or in gait and of Hallux Valgus axial deviations, with the surgical possibilities of correcting this pathology, developing in particular the proximal opening-wedge osteotomy of the first metatarsal.

In conclusion, **the main objective** of the thesis is to conduct experimental and generalized CAD-CAE researches aiming to study the foot biomechanics in general and Hallux Valgus deviation with surgical corrective variants in detail.

The goal is to optimise the proximal opening-wedge osteotomy of the first metatarsal, to achieve precise and correct geometric planning, with a focus on the stability of the surgical area, an efficient post-operative recovery and to prevent cracks during the opening process.

Furthermore, in line with the studies and researches approached at theme level, through this PhD thesis we aim to achieve certain aspects of interest, consequently, the main objective is achieved by materializing the following objectives:

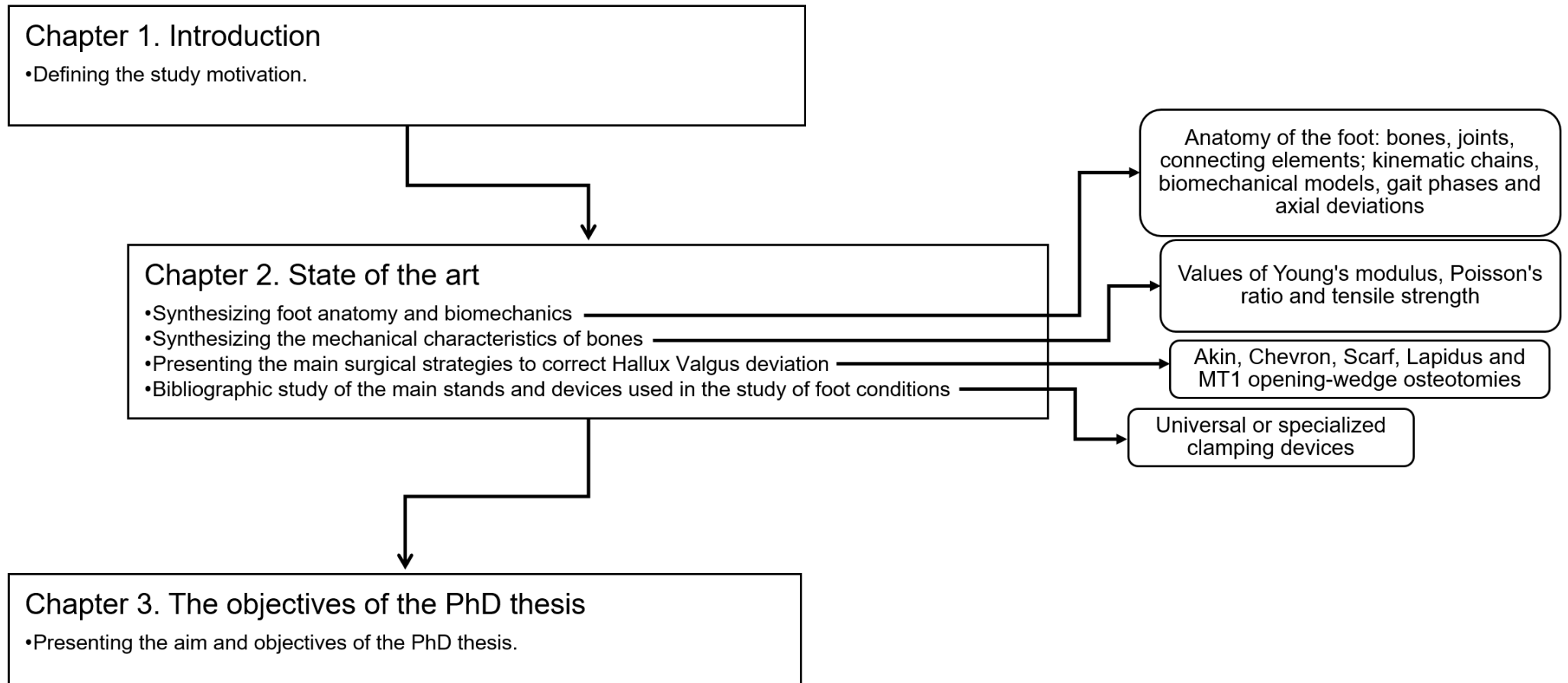
1. Synthetizing of the state-of-the-art of studies on surgical strategies for the correction of Hallux Valgus axial deviations, computer-assisted approaches to the problem and experimental studies in the field;
2. 3D modelling of certain bones of the foot, respectively those affected by Hallux Valgus deviation (first metatarsal and proximal phalanx), taking into account their real structure, using the concept of constructive-anatomical entity;
3. Development of the generalised and parameterised assembly of the human ankle-foot structure, allowing the reproduction of the six basic movements of the foot, using the Skeleton Systems method;
4. Development of the parameterised foot assembly for modelling the three phases of gait using the Skeleton Systems method;
5. Development of a parametrized assembly of the proximal phalanx of the hallux, the distal phalanx of the hallux, the first two metatarsals and the medial cuneiform, allowing CAD generation of the three forms of Hallux Valgus disease: mild, moderate and severe;

6. Generalised modelling of the five main types of surgical procedures related to the correction of Hallux Valgus disease: Akin, Chevron, Scarf, Lapidus and proximal opening-wedge osteotomy of the first metatarsal;
7. Numerical simulation of the corrective angulation process specific for the proximal opening-wedge osteotomy of the first metatarsal, using different CORA positions to perform this procedure;
8. Design and manufacture of a specialized clamping device for performing experimental research, writing a CNC program for simulating osteotomies and validating the working methodology using bone replicas developed by additive manufacturing methods;
9. Conducting experimental research on the displacements and maximum openings of several variants of osteotomy arrangement for opening the first metatarsal and experimental validation of the numerical research.

In terms of methods and tools used, the following can be listed:

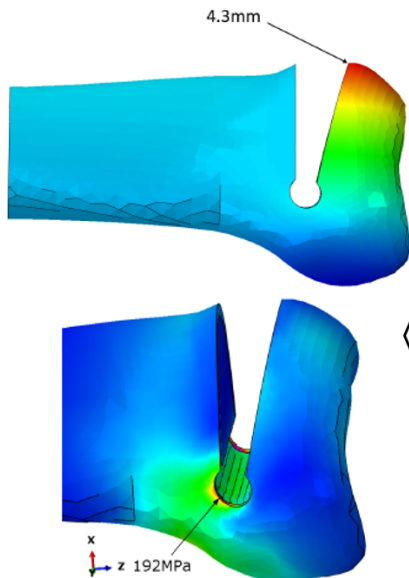
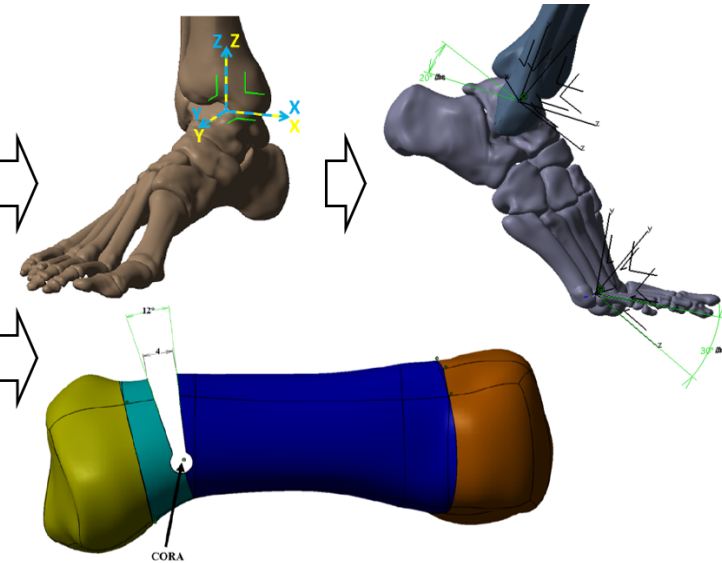
- The use of CATIA V5 software for the development of models of real structures and assemblies corresponding to the Skeleton systems method;
- Parameterisation of the assemblies by linking the 3D structures with the corresponding Microsoft spreadsheets, more precisely Excel;
- Use of the Dassault Systemes suite for the development of numerical simulations, via ABAQUS 2020;
- Design algorithms and experimental modelling;
- Interpreting the experimental data using STATISTICA 12.5 and Minitab 18 software.

The graphical algorithm of the PhD thesis



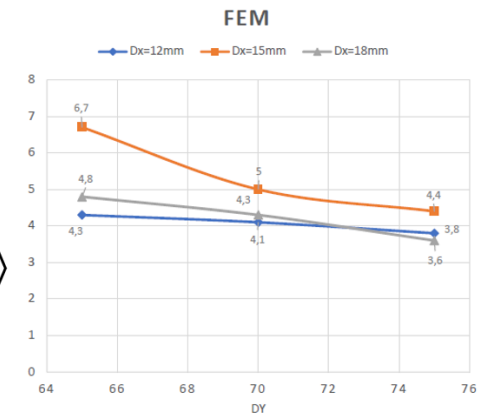
Chapter 4. CAD modelling of the osteoarticular complex of the human foot

- 3D modeling of MT1 and proximal phalanx based on geometric entities;
- 3D modelling of MT1 and proximal phalanx considering their real structure;
- Development of a fully parameterized generalized CAD assembly of the foot, allowing the generation of main and intermediate phases of gait, basic and associated foot movements and pathological situations;
- Simulation of the five main types of surgery to correct Hallux Valgus deviation: Akin, Scarf, Chevron, Lapidus and proximal opening-wedge osteotomy of the first metatarsal.



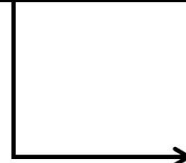
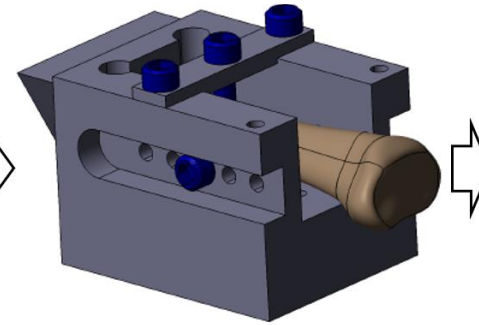
Chapter 5. Numerical simulations of osteotomies for the correction of the Hallux Valgus axial deviations

- Studying the behaviour of the first metatarsal during correction angulation, a specific step of the proximal opening-wedge osteotomy of the first metatarsal. In this study, the aim was to optimise the CORA position to avoid microcracks during angulation for 9 positioning variants;
- The specific steps of a static FEM analysis were carried out, the response functions considered being: maximum opening, the values of the equivalent Von Mises stresses at 2, 4, 5 and 6 mm opening and the shear stresses at maximum opening;
- 2D and 3D graphical representations were made for the maximum opening, which is the most important response function in the FEM study, being a concrete and palpable indicator for surgeons to avoid microcracks in the CORA. It can be concluded in this regard that the best openings are obtained for $Dx=15mm$ regardless of the value of Dy . For $Dx=12mm$ and $Dx=18mm$ the values are fairly close to each other being grouped around 4mm.



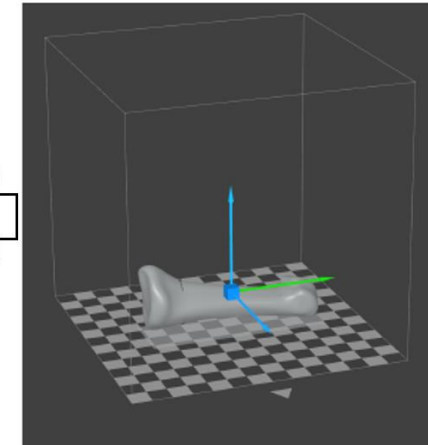
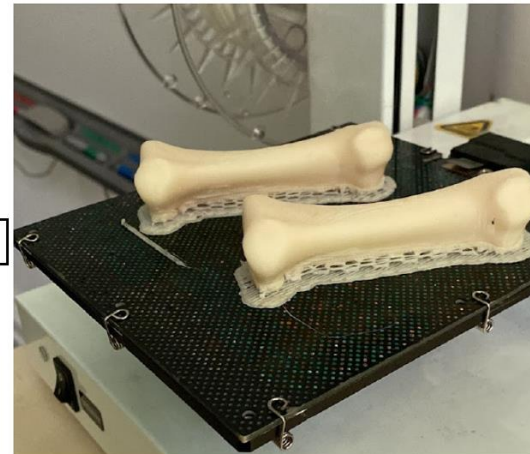
Chapter 6. Design and manufacture of a specialised clamping device for carrying out the experimental research

- The requirements to be met by the device and the experimental objectives that can be achieved with such a stand have been highlighted, resulting in the main functions that it should provide;
- Constructive solutions for each function have been considered and designed, resulting in a modular device with good flexibility and wide possibilities of use.



Chapter 7. The use of additive technologies for the study of Hallux Valgus axial deviations

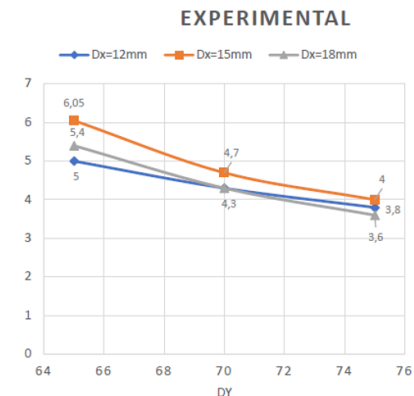
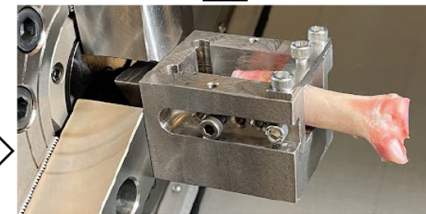
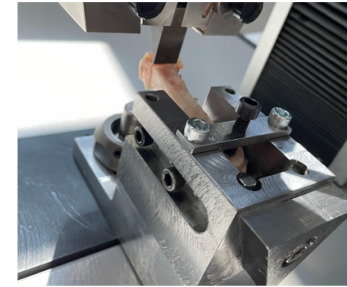
- Bone replicas of human and porcine metatarsals have been developed by Additive Manufacturing in two variants: from ABS by the FDM method and from resin by the SLA method.



Chapter 8. Experimental research on the proximal opening-wedge osteotomy of the first metatarsal

- Experimental research was carried out to validate the results obtained from finite element analysis;
- Technological equipment used: Haas ST-15Y CNC lathe, for machining the osteotomy plane and the CORA hole and Galdabini Quasar 25 tensile-compression machine for the angular correction;
- A preliminary experiment was carried out, on printed bones, in which the osteotomy plane and the hole in the CORA were machined on the mentioned machine, according to the position recommended in the literature;
- After the validation of the preliminary experiment, the input (independent) variables D_x and D_y were established, which characterize the experimental object under investigation, in accordance with the geometric planning of the proximal opening wedge metatarsal osteotomy;
- Three levels of variation were established for each variable (D_x - 12, 15 and 18 mm; D_y - 65, 70 and 75%). A full factorial experimental program was designed, resulting in nine experimental trials, which achieved the combination of all levels of variation of the variables;
- Real porcine specimens were prepared corresponding to two replicates of each experimental point, 18 specimens being required for as many experiments;
- The 18 experiments were performed sequentially, obtaining for each of them the force-displacement diagrams, the maximum force and the maximum opening of the osteotomy wedge;
- Data was collected for both maximum force and maximum aperture on a spreadsheet basis for the 18 planned experiments. The following values of mean, standard deviation, coefficient of variation and empirical dispersion were obtained for the nine experimental trials for each of the two response functions;
- The variation of the maximum force in relation to the input variables D_x and D_y was also performed by two suggestive graphical representations (2D and 3D) made with the STATISTICA12 software. With the same program a second-degree regression equation of the maximum force as a function of the input variables was also determined;
- Graphical representations (2D and 3D) were made showing the variation of the response function in relation to the input variables D_x and D_y , showing that the best openings are obtained when the osteotomy plane is positioned at $D_x=15\text{mm}$, and that the largest of these, 6.05 mm, is achieved in the combination $D_x=15\text{mm}$, $D_y=65\%$;
- A parallel analysis of the variations of the maximum openings obtained by FEM with the experimental ones under the same test conditions was also carried out, from which it resulted that the proposed experiment validates very well the numerical analysis performed and thus, one of the experimental objectives was achieved;
- Due to the importance of the response function, an experimental modelling of the investigated phenomenon was also performed. The homogeneity check of the dispersion of the objective function d_{max} was evaluated in the model, confirming the homogeneity of the response function for the 9 trials, the reproducibility dispersion and the linear regression model were calculated;
- The significance of the coefficients of the regression equation was checked, resulting that all the coefficients of the regression equation are significant with the specification that D_y has a much more important weight in the regression equation than the coefficient of D_x . Regarding the model adequacy, following specific calculations, it resulted that the experimental model is adequate and represents the coverage of the experimental phenomenon studied;
- The ANOVA analysis performed for the whole experimental model and the residuals analysis was carried out using Minitab18 software and confirmed that the objective function can be controlled using the experimental model carried out, which gives a very good degree of generality and applicability for the experimental field investigated.

Chapter 9. General conclusions. Personal contributions. Future research directions.





General conclusions. Personal contributions. Future research directions.

The scientific approach carried out is driven by the need for in-depth engineering studies that have a direct effect on the optimization of Hallux Valgus surgical interventions, by the social impact that the results might have, given the high frequency of occurrence of the condition, but also by the idea of interdisciplinarity, which has proven that the results obtained interdisciplinarily are much better than those obtained by the separate approaches of the two fields, medical and engineering.

The development of a geometric surgery planning guide for orthopaedic surgeons, with which, for example, an appropriate choice of CORA layout can be made, has important effects on the stability of the surgery site and post-operative recovery.

Also, the development of the generalised CAD-CAE models can be of great benefit to future research in the field.

Based on an ample bibliographical documentation, we can state that the thesis is in line with the studies and research in the field, worldwide.

Personal contributions

Through this PhD thesis, numerous original contributions have been made in terms of modelling the foot biomechanics and optimising surgical interventions of correction of the Hallux Valgus condition, the most notable of which are highlighted as per:

- Elaborating a foot anatomy study and transposing the problem into the engineering area;
- Synthesizing the mechanical characteristics of human (cortical-trabecular) and animal (bovine and porcine) bone structures;
- Identifying biomechanical research areas within the foot area and its axial deviations;
- Setting up the Gcs and Tcs reference systems for parametric CAD modelling using Skeleton systems;
- Transposing the main foot joints into classical mechanical friction joints (plane, ellipsoidal, cylindrical etc.);
- Identifying the optimal positioning of the ankle reference system origin (talocrural joint) and the main geometric elements (axes, angles), with respect to which the foot movements and gait phases will be modelled;
- Identifying the geometric and dimensional elements useful in the 3D gait modelling, including the angular elements needed for CAD modelling of axial deviations;

- Identifying the geometric, dimensional and reference system elements that will allow the 3D modelling of the five types of Hallux Valgus correction surgeries;
- Making distinct 3D models for the body, head and base of the proximal phalanx and the first metatarsal and assembling them, as well as distinct CAD models for the cortical and cancellous zones of these bones, in accordance with the constructive-anatomical entities method;
- Elaborating the parameterized foot assembly for generating the pathologies that may occur in the orthostatic position and the basic and associated movements. Necessary reference systems, origins and axes definition and fitting them within the Skeleton systems;
- Taking into account the three levels of severity of Hallux Valgus condition, three variants of the Hallux Valgus axial deviation models were developed, considering the congruency status of the first metatarsophalangeal joint (congruent, deviated or subluxated joint);
- 3D modelling and virtual simulation of the five main types of Hallux Valgus surgeries: Akin, Scarf, Chevron, Lapidus and proximal opening wedge metatarsal osteotomy, using the parameterized CAD models of axial deviations previously developed;
- CAE studies on proximal opening wedge metatarsal osteotomy and CORA positioning optimization;
- Developing a script to automatically generate the results of the 9 numerical simulations, combining the 3 levels of variation of the 2 variables used in the analysis;
- For the resulting parameter (d), regarding the maximum opening wedge opening, 2D and 3D variation graphs were plotted;
- Design and manufacture of a specialized device for experimental research of the proximal opening wedge metatarsal osteotomy;
- Manufacturing of bone replicas by additive manufacturing methods, for the development of the preliminary experiment to validate the experimental methodology;
- Design and implementation of an experimental research program to study the behaviour during angular correction of the first metatarsal in different variations of its opening osteotomy arrangement;
- Development of a CNC program for NC machining for proximal opening wedge metatarsal osteotomy;
- A full factorial experimental program was designed in which the response functions were the maximum force F_{max} and the maximum osteotomy wedge opening d_{max} , where the influence factors were Dx and Dy ;
- The variation of force in relation to the displacement (therefore the maximum osteotomy wedge opening) was determined in relation to the influencing factors Dx and Dy ;
- The collected results were presented in the three common forms: tables, graphs (2D and 3D) and mathematical relations;

- A processing of the obtained data was carried out with the establishment of the regression model, verification of the dispersion homogeneity of the response function, calculation of the coefficient's significance of the regression equation and confirmation of the adequacy of the model;
- An ANOVA analysis was performed for the whole experimental model, an analysis of residuals and correlation coefficients showing that the objective function can be controlled with the elaborated experimental model.

Future research directions

Starting from the results obtained within this PhD thesis, studies can be extended in the following research directions:

- Based on the generalized model of the foot, studies can be made regarding the compressive stresses of the metatarsal bones or phalanges during walking even a study of the behaviour of post-operative structures in various phases of walking;
- Similar approaches to those in this thesis can be made using the Hallux Valgus deviations CAD models of the other four types of operations presented;
- Using the CAD models for the development of customized orthoses or prostheses for the conservative treatment of the Hallux Valgus condition;
- The microscope study of the angular correction of the first metatarsal, for the accurate establishment of the critical moment of the microcracks appearance;
- Completing the present study regarding the optimization of the geometric planning of the first metatarsal opening osteotomies by choosing another set of parameters: Dx values from 0.5 to 0.5mm and Dy from percentage to percentage, applied around the critical values obtained in this thesis;
- Development of customized Hallux Valgus non-invasive correction devices, executed by additive manufacturing;
- Design and development of innovative position preservation devices for the post-angulation configuration within the proximal opening wedge metatarsal osteotomy;
- Approaching the topic for different mechanical characteristics of bones affected by natural aging or other causes.

References

- [1] M. Nedeș și N. Nedeș, Anatomia și fiziologia omului, MERIDIANE PUBLISHING, 2016.
- [2] C. T. Niculescu, R. Carmaciu, B. Voiculescu, C. Salavastru, C. Nita și C. Ciornei, Anatomia și fiziologia omului - Compendiu, Editura Corint, 2014.
- [3] I. I. Cofaru, „Cercetări privind biomecanica deviațiilor axiale ale membrului inferior uman și dezvoltarea unor echipamente chirurgicale aferente,” Sibiu, 2013.
- [4] J. Herring, Tachdjian's pediatric orthopaedics, 4th edn, Elsevier, 2007.
- [5] A. G. Lupu, Studiu anatomoclinic al piciorului, din perspectiva antropologică, București, 2018.
- [6] V. Papilian, Anatomia Omului. Aparatul locomotor. Vol I (editia a XII-a), Editura ALL, 2008.
- [7] A. Naderi, „Medial cuneiform bone,” *Cuneiform. OrthopaedicsOne Review. In: OrthopaedicsOne - The Orthopaedic Knowledge Network*, 2010.
- [8] G. A. Piersol, Human Anatomy, Philadelphia: J. B. Lippincott Company, 1908.
- [9] A. Ahn și A. J. Grodzinsky, „Relevance of collagen piezoelectricity to “Wolff's Law”: A critical review,” *Medical Engineering & Physics*, vol. 31, nr. 7, pp. 733-741, 2009.
- [10] J.-Y. Rho, L. Kuhn-Spearing și P. Zioupos, „Mechanical properties and the hierarchical structure of bone,” *Medical Engineering & Physics*, vol. 20, nr. 2, pp. 92-102, 1998.
- [11] K. Tao, D. Wang, C. Wang, X. Wang, A. Liu, C. J. Nester și D. Howard, „An In Vivo Experimental Validation of a Computational Model of Human Foot,” *Journal of Bionic Engineering*, vol. 6, nr. 4, pp. 387-397, 2009.
- [12] D. Wu, P. Isaksson, S. J. Ferguson și C. Persson, „Young's modulus of trabecular bone at the tissue level: A review,” *Acta Biomaterialia*, vol. 78, pp. 1-12, 2018.
- [13] H. Andra, S. Battiato, G. Bilotta, G. M. Farinella, G. Impoco, J. Orlik, G. Russo și A. Zemitis, „Structural Simulation of a Bone-Prosthesis System of the Knee Joint,” *PMID: 27873848; PMCID: PMC3705538*, 2008.
- [14] M. F. A. Akhbar și A. R. Yusoff, „Comparison of bone temperature elevation in drilling of human, bovine and porcine bone,” *17th CIRP Conference on Modelling of Machining Operations*, vol. 82, pp. 411-414, 2019.
- [15] L. Feng, M. Chittenden, J. Schirer, M. Dickinson și I. Jasiuk, „Mechanical properties of porcine femoral cortical bone measured by nanoindentation,” *Journal of Biomechanics*, vol. 45, pp. 1775-1782, 2012.
- [16] C. A. Luo, S. Y. Hua, S. C. Lin, C. M. Chen și C. S. Tseng, „Stress and stability comparison between different systems for high tibial,” *BMC Musculoskelet. Disord.*, vol. 14, 2013.
- [17] C. A. Luo, S. C. Lin, S. Y. Hwa, C. M. Chen și C. S. Tseng, „Biomechanical effects of plate area and locking screw on medial open,” *Comput. Methods Biomech. Biomed*, vol. 18, pp. 1263-1271, 2015.
- [18] C. E. Hoffler, K. E. Moore, K. Kozloff, P. K. Zysett și S. A. Goldstein, „Age, gender, and bone lamellae elastic moduli,” *J. Orthop. Res.*, vol. 18, pp. 432-437, 2000.

- [19] I. I. Cofaru, M. Oleksik, N. F. Cofaru, A. H. Branescu, A. Hasegan, M. D. Roman, S. R. Fkeaca și R. D. Dobrotra, „A Computer-Assisted Approach Regarding the Optimization of the Geometrical Planning of Medial Opening Wedge High Tibial Osteotomy,” *Applied Sciences - MDPI*, vol. 12, pp. 1-22, 2022.
- [20] A. Williams și C. Nester, *Pocket Podiatry: Footwear and Foot Orthoses*, CHAPTER 1 - Principles of foot biomechanics and gait, Salford: Churchill Livingstone, 2010.
- [21] A. Perrier, V. Luboz, M. Bucki, F. Cannard, N. Vuillerme, Y. Payan și J. Ohayon, „Chapter 25 - Biomechanical Modeling of the Foot,” în *Biomechanics of Living Organs*, Grenoble, France, Academic Press, 2017, pp. 545-563.
- [22] A.-A. Najefi, K. Malhotra și A. Goldberg, „Mechanical and anatomical axis of the lower limb in total ankle arthroplasty,” *The foot*, vol. 44, 2020.
- [23] R. A. Siston, A. C. Daub, N. Giori, S. Goodman și S. Delp, „Evaluation of Methods That Locate the Center of the Ankle for Computer-assisted Total Knee Arthroplasty,” *Clinical Orthopaedics and Related Research*, vol. 439, pp. 129-135, 2005.
- [24] E. T. Avramescu, *Bazele anatomice ale mișcării*, Târgu-Mureș, 2010.
- [25] L. Seres-Sturm, K. Brinzaniuc, C. Nicolescu și R. Sipos, *Anatomia membrilor*, Târgu-Mureș: Editura UNIVERSITY PRESS (UMF) , 2007.
- [26] S. Delacroix, *Évaluation des effets cinématiques et dynamiques induits par le port d'orthèses plantaires lors de la marche*, Lyon, 2015.
- [27] S. Angin și I. Demirbucen, „Ankle and foot complex,” *Comparative Kinesiology of the Human Body*, pp. 411-439, 2020.
- [28] C. W. Chan și A. Rudins, „Foot biomechanics during walking and running,” vol. 69, nr. 5, pp. 448-461, 1994.
- [29] M. W. Chapman, R. M. Szabo, R. Marder, K. G. Vince, R. A. Mann, J. M. Lane, R. F. McLain și G. Rab, *Chapman's Orthopaedic Surgery* 3rd edition, Lippincott Williams & Wilkins Publishers, 2001.
- [30] S. P. Pop, I. Gergely, O. M. Russu și C. O. Roman, *Elemente de ortopedie ed. II*, Târgu-Mureș: UNIVERSITY PRESS , 2013.
- [31] R. A. Donatelli, „Normal biomechanics of the foot and ankle,” *J Orthop Sports Phys Ther*, vol. 7, nr. 3, pp. 91-95, 1985.
- [32] A. Steindler, *Kinesiology: Of the Human Body Under Normal and Pathological Conditions*, Charles C Thomas Pub Ltd, 1977.
- [33] M. N. Mojica și J. S. Early, *Foot Biomechanics - Atlas of Orthoses and Assistive Devices*, Elsevier, 2019.
- [34] Y. Wang, D. W.-C. Wong și M. Zhang, „Computational Models of the Foot and Ankle for Pathomechanics and Clinical Applications: A Review,” *Annals of Biomedical Engineering*, vol. 44, nr. 1, pp. 213-221, 2016.
- [35] D. W.-C. Wong, Y. Wang, M. Zhang și A. K.-L. Leung, „Functional restoration and risk of non-union of the first metatarsocuneiform arthrodesis for hallux valgus: A finite element approach,” *Journal of Biomechanics*, vol. 48, nr. 12, pp. 3142-3148, 2015.
- [36] S. Scott și D. A. Winter, „Biomechanical model of the human foot: Kinematics and kinetics during the stance phase of walking,” *Journal of Biomechanics*, vol. 26, nr. 9, pp. 1091-1104, 1993.

- [37] K. G. Gruben și W. L. Boehm, „Force direction pattern stabilizes sagittal plane mechanics of human walking,” *Human Movement Science*, vol. 31, nr. 3, pp. 649-659, 2012.
- [38] C. Radu, „DETERMINAREA FORȚELE DE REACTIUNE DIN ARTICULATIA GLEZNEI ÎN CONDIȚII DINAMICE,” *ANNALS of the ORADEA UNIVERSITY*, pp. 386-391.
- [39] H. A. Jacob, „Forces acting in the forefoot during normal gait--an estimate,” *Clinical Biomechanics*, vol. 16, nr. 9, pp. 783-792, 2001.
- [40] A. Bryant, P. Tinley și K. Singer, „A Comparison of Radiographic Measurements in Normal, Hallux Valgus, and Hallux Limitus Feet,” *The Journal of Foot & Ankle Surgery*, vol. 39, nr. 1, pp. 39-43, 2000.
- [41] S. Srivastava, N. Chockalingam și T. Fakhri, „Radiographic Angles in Hallux Valgus: Comparison between Manual and Computer-Assisted Measurements,” *The Journal of Foot & Ankle Surgery*, vol. 49, pp. 523-528, 2010.
- [42] H. Xu, K. Jin, Z. Fu, M. Ma, Z. Liu, S. An și B. Jiang, „Radiological Characteristics and Anatomical Risk Factors in the Evaluation of Hallux Valgus in Chinese Adults,” *Chinese Medical Journal*, vol. 128, nr. 1, 2015.
- [43] R. Meary, „On the measurement of the angle between the talus and the first metatarsal,” *Rev Chir Orthop* 53:389, 1967.
- [44] J. M. Linklater, J. W. Read și C. L. Hayter, „Imaging of the Foot and Ankle,” *Techniques in Foot & Ankle Surgery*, vol. 7, nr. 3, 2008.
- [45] N. F. Cofaru și A. H. Brănescu, „A review on biomechanics of the hallux valgus pathology and its surgical treatments,” *COSME*, vol. 1009, 2020.
- [46] E. M. Escobedo, S. J. Pinnley, J. C. Hunter și B. J. Sangeorzan, *Evaluation of Adult Foot Alignment*, Sacramento, California, 2016.
- [47] J. Gui, X. Gu și M. Hou, „X- ray evaluation of the normal and hallux valgus feet and its clinical values,” *Chinese Journal of Orthopaedics*, vol. 12, 2001.
- [48] G. LaPorta, T. Melillo și D. Olinsky, „X-ray evaluation of hallux abducto valgus deformity,” *Journal of the American Podiatry Association*, vol. 64, nr. 8, pp. 544-566, 1974.
- [49] F. Condon, M. Kaliszer, D. Conhyea, T. O'Donell, A. Shaju și E. Materson, „The first intermetatarsal angle in hallux valgus: an analysis of measurement reliability and the error involved.,” *Foot Ankle Int*, vol. 23, pp. 717-721, 2002.
- [50] A. H. Brănescu, I. C. Lebădă, V. Mihuț, N. Marjanovic și M. Rackov, „CAD modelling of the human femur taking into account the structure of the bone,” *10th International Conference on Manufacturing Science and Education – MSE 2021 - MATEC Web Conf.*, 2021.
- [51] L. Voo, „Stress fracture risk analysis of the human femur based on computational biomechanics,” *Johns Hopkins APL Technical Digest (Applied Physics Laboratory)*, vol. 25, nr. 3, 2004.
- [52] M. Peacock, D. L. Koller, D. Lai, S. Hui, T. Foroud și M. J. Econs, „Sex-specific quantitative trait loci contribute to normal variation in bone structure at the proximal femur in men,” *Bone*, vol. 37, pp. 467-473, 2005.

- [53] P. D. Brîndașu, I. I. Cofaru, N. F. Cofaru și L. Roman, „Computer Simulation Paradigm Regarding the Structure and Mechanical Characteristics of Human Long Bones,” *Advanced Materials Research*, vol. 814, pp. 99-103, 2013.
- [54] I. I. Cofaru și E. I. Huzu, „Generalized Modelling of the human lower limb assembly,” *The 1st International Conference for Doctoral Students*, 2013.
- [55] I. I. Cofaru, „Biomechanic of the opening tibial osteotomy,” *Fascicle of Management and Technological Engineering*, nr. 1, 2014.
- [56] A. C. Merchant, R. Fraiser, J. Dragoo și M. Fredericson, „A reliable Q angle measurement using a standardized protocol,” *The Knee*, vol. 27, nr. 3, pp. 934-939, 2020.
- [57] P. Berce, N. Bâlc, R. Păcurar, S. Brătean, C. Caizar, A. S. Radu și I. Fodorean, *Tehnologii de fabricatie prin adaugare de material si aplicatiile lor*, Cluj-Napoca: Editura Academiei Romane, 2014.
- [58] A. H. Brănescu, *Proiectarea, dezvoltarea și fabricarea reperului Skid Plate*, Sibiu, 2017.
- [59] R. E. Petrus, B. Johnson și I. Bondrea, „A low budget, reverse engineering solution for obtaining functional parts,” *Academic Journal of Manufacturing Engineering*, vol. 13, nr. 2, pp. 78-83, 2015.
- [60] G. O. Karabicak, N. Bek și U. Tiftikci, „SHORT-TERM EFFECTS OF KINESIOTAPING ON PAIN AND JOINT ALIGNMENT IN CONSERVATIVE TREATMENT OF HALLUX VALGUS,” *Journal of Manipulative and Physiological Therapeutics*, vol. 38, nr. 8, pp. 564-571, 2015.
- [61] J. Ferrari, J. P. Higgins și T. D. Prior, „Interventions for treating hallux valgus (abductovalgus) and bunions,” *Cochrane Database Syst Rev*, 2004.
- [62] R. A. Mann și M. J. Coughlin, „Adult hallux valgus,” *Surgery of the foot and ankle (7th ed.)*, pp. 159-269, 1999.
- [63] S. T. Canale, F. M. Azar, J. H. Beaty și W. C. Campbell, *Campbell's operative orthopaedics*, Thirteenth edition, Philadelphia, PA : Elsevier, Inc., 2017.
- [64] L. Fraisser, C. Konrads, M. Hoberg, M. Rudert și M. Walcher, „Treatment of hallux valgus deformity,” *EFORT Open Rev*, pp. 295-302, 2016.
- [65] J. L. Beskin, „Akin's phalangeal osteotomy for bunion repair,” în *Current therapy in foot and ankle surgery*, St. Louis, Mosby, 1993.
- [66] K. H. Kristen, C. Berger și S. Stelzig, „The scarf osteotomy for the correction of hallux valgus deformities,” *Foot & Ankle International*, vol. 23, nr. 3, pp. 221-229, 2002.
- [67] S. Jones, H. A. Al Hussainy, F. Ali, R. P. Betts și M. J. Flowers, „Scarf osteotomy for hallux valgus: a prospective clinical and pedobarographic study,” *The Journal of Bone and Joint Surgery. British volume*, Vol. %1 din %286-b, nr. 6, 2004.
- [68] J. C. Coetzee și R. Pascal, „Surgical Strategies: Scarf Osteotomy for Hallux Valgus,” *FOOT & ANKLE INTERNATIONAL*, vol. 28, nr. 4, pp. 529-535, 2004.
- [69] S. S. Suresh, „Scarf osteotomy - Is it the procedure of choice in hallux valgus surgery? A preliminary report,” *Oman Med J.*, vol. 22, nr. 3, pp. 47-50, 2007.
- [70] A. H. Waly și M. G. Morsy, „Scarf osteotomy in severe hallux valgus deformity,” *The Egyptian Orthopaedic Journal*, vol. 54, pp. 15-20, 2019.

- [71] H. W. Park și S. J. Kim, „Treatment Results of Hallux Valgus Deformity by Parallel-Shaped Modified Scarf Osteotomy,” *J Korean Foot Ankle Soc.*, vol. 16, nr. 2, pp. 123-127, 2012.
- [72] M. Jager, M. Schmidt, A. Wild, B. Bittersohl, S. Courtois, T. G. Schmidt și K. Rudiger, „Z-osteotomy in hallux valgus: clinical and radiological outcome after scarf osteotomy.,” *Orthop Rev (Pavia)*, vol. 30, nr. 1, 2009.
- [73] S. E. Smith, K. B. Landorf, P. A. Butterworth și H. B. Menz, „Scarf versus Chevron Osteotomy for the Correction of 1–2 Intermetatarsal Angle in Hallux Valgus: A Systematic Review and Meta-analysis,” *The Journal of Foot & Ankle Surgery*, vol. 51, pp. 437-444, 2012.
- [74] E. Swanton, L. Mason și A. Malloy, „How Do I Use the Scarf Osteotomy to Rotate the Metatarsal and Correct the Deformity in Three Dimensions?,” *Foot Ankle Clin N Am*, vol. 23, pp. 239-246, 2018.
- [75] S. P. Adam, S. C. Choung, Y. Gu și M. J. O`Malley, „Outcomes after Scarf Osteotomy for Treatment of Adult Hallux Valgus Deformity,” *Clinical Orthopaedics and Related Research*, vol. 469, nr. 3, pp. 854-859, 2011.
- [76] K. W. Young, H. S. Lee și S. C. Park, „Modified Proximal Scarf Osteotomy for Hallux Valgus,” *Clinics in orthopedic surgery*, vol. 10, nr. 4, pp. 479-483, 2018.
- [77] H. J. Trnka și P. Bock, „Scarf Osteotomy for Correction of Hallux Valgus,” în *Operative Techniques: Foot and Ankle Surgery (Second Edition)*, 2018, pp. 15-25.
- [78] B. J. Sangeorzan și S. T. Hansen, „Modified Lapidus Procedure for Hallux Valgus,” *Foot & Ankle*, vol. 9, nr. 6, 1989.
- [79] C. F. Hyer, G. Berlet, T. Lee și E. Orhner, *DARCO BOW Plate SURGICAL TECHNIQUE*, Wright Medical Technology Inc., 2017.
- [80] J. U. Wester, E. Hamborg-Petersen, N. Herold, P. B. Hansen și J. Froekjaer, „Open wedge metatarsal osteotomy versus crescentic osteotomy to correct severe hallux valgus deformity – A prospective comparative study,” *Foot and Ankle Surgery*, vol. 22, nr. 1, pp. 26-31, 2016.
- [81] W. D. Wai-Chi, *Biomechanics of Hallux Valgus and Evaluation of Interventions PhD thesis*, Hong-Kong, 2013.
- [82] H. J. Trnka, B. G. Parks, G. Ivanic, I. T. Chu, M. E. Easley, L. C. Schon și M. S. Myerson, „Six first metatarsal shaft osteotomies: mechanical and immobilization comparisons,” *Clinical orthopaedics and related research*, vol. 381, pp. 256-265, 2000.
- [83] J. I. Acevedo, V. J. Sanmarco, H. R. Boucher, B. G. Parks, L. C. Schon și M. S. Myerson, „Mechanical comparison of cyclic loading in five different first metatarsal shaft osteotomies.,” *Foot Ankle Int*, vol. 23, nr. 8, pp. 711-716, 2002.
- [84] E. D. Stamatis, D. O. Navid, B. G. Parks și M. S. Myerson, „Strength of fixation of Ludloff metatarsal osteotomy utilizing three different types of Kirschner wires: a biomechanical study,” *Foot and Ankle International*, vol. 24, nr. 10, pp. 805-811, 2003.
- [85] I. Popoff, J. P. Negrine, M. Zecovic, M. Svehla și W. R. Walsh, „The effect of screw type on the biomechanical properties of SCARF and crescentic osteotomies of the first metatarsal.,” *The Journal of foot and ankle surgery*, vol. 42, nr. 3, pp. 161-164, 2003.

- [86] K. Jacobson, A. Gough, S. S. Mendicino și M. S. Rockett, „Mechanical comparison of fixation techniques for the offset V osteotomy: a saw bone study.,” *The Journal of foot and ankle surgery*, vol. 42, nr. 6, pp. 339-343, 2003.
- [87] M. Bozkurt, C. Tigarar, M. Dalstra, N. C. Jensen și F. Linde, „Stability of a cannulated screw versus a Kirschner wire for the proximal crescentic osteotomy of the first metatarsal: a biomechanical study,” *J Foot Ankle Surg*, vol. 43, nr. 3, pp. 138-143, 2004.
- [88] H. G. Jung, G. P. Guyton, B. G. Parks, K. J. Dom, A. Nguyen și L. C. Schon, „Supplementary axial Kirschner wire fixation for crescentic and Ludloff proximal metatarsal osteotomies: a biomechanical study,” *Foot & ankle international*, vol. 26, nr. 8, pp. 620-626, 2005.
- [89] C. Jones, M. Coughlin, W. Petersen, M. Herbot și J. Paletta, „Mechanical comparison of two types of fixation for proximal first metatarsal crescentic osteotomy,” *Foot Ankle Int*, vol. 26, nr. 5, pp. 371-374, 2005.
- [90] P. Vienne, P. Favre, D. Meyer, R. Scoeniger, S. Wirth și N. Espinosa, „Comparative mechanical testing of different geometric designs of distal first metatarsal osteotomies,” *Foot and Ankle International*, vol. 28, nr. 2, pp. 232-236, 2007.
- [91] S. G. Hofstaetter, R. R. Glisson, C. J. Alitz, H. J. Trnka și M. E. Easley, „Biomechanical comparison of screws and plates for hallux valgus opening-wedge and Ludloff osteotomies,” *Clinical Biomechanics*, vol. 23, nr. 1, pp. 101-108, 2008.
- [92] A. M. Unal, O. Baran, B. Uzun și A. C. Turan, „Comparison of screw-fixation stabilities of first metatarsal shaft osteotomies: a biomechanical study,” *Acta Orthop Traumatol Turc*, vol. 44, nr. 1, pp. 70-75, 2010.
- [93] P. Favre, M. Farine, J. G. Snedeker, G. J. Maquieira și N. Espinosa, „Biomechanical consequences of first metatarsal osteotomy in treating hallux valgus,” *Clinical Biomechanics*, vol. 25, nr. 7, pp. 721-727, 2010.
- [94] S. P. Tsilikas, E. D. Stamatis, S. K. Kourkoulis, A. S. Mitousoudis, P. E. Chatzistergos și P. J. Papagelopoulos, „Mechanical Comparison of Two Types of Fixation for Ludloff Oblique First Metatarsal Osteotomy,” *The Journal of foot and ankle surgery*, vol. 50, nr. 6, pp. 699-702, 2011.
- [95] S. P. Gocke, F. J. Rottier, R. M. Havey, S. M. Renner, A. G. Patwardhan și G. Carandang, „Quantitative Analysis of the Long-and Short-arm Crescentic Shelf Bunionectomy Osteotomies in Fresh Cadaveric Matched Pair Specimens,” *The Journal of foot and ankle surgery*, vol. 50, nr. 2, pp. 158-164, 2011.
- [96] „<https://www.sawbones.com/foot-large-left-first-metatarsal-4th-generation-composite-3422.html>,” [Interactiv].
- [97] B. Yin, J. Guo, J. Wang, S. Li, Y. Liu și Y. Zhang, „Bone Material Properties of Human Phalanges Using Vickers Indentation,” *Orthopaedic Surgery*, vol. 11, nr. 3, pp. 487-492, 2019.
- [98] J. Bucha, „Utilization and advantages of skeleton modelling in Catia Environment,” în *Industrial research into the methods and procedures in generative design and knowledge engineering in car development*, BRATISLAVA, 2014.
- [99] I. I. Cofaru, „The CAD modelling of the human tibia affected by form deviations,” *Fascicle of Management and Technological Engineering*, nr. 1, 2014.

- [100] N. F. Cofaru, A. H. Brănescu, V. Marjanovic și M. Blagojevic, „Contributions regarding 3D modelling of biomechanics of the foot,” *MATEC Web of Conferences* 343, 04009 - 10th International Conference on Manufacturing Science and Education, 2021.
- [101] N. F. Cofaru și A. H. Brănescu, „CONTRIBUTIONS IN 3D GEOMETRIC MODELING OF THE HALLUX VALGUS AXIAL DEVIATION,” *ACADEMIC JOURNAL OF MANUFACTURING ENGINEERING*, vol. 18, nr. 4, 2020.
- [102] C. d. C. Netto și M. Richter, „Use of Advanced Weightbearing Imaging in Evaluation of Hallux Valgus,” *Foot and Ankle Clinics*, vol. 25, nr. 1, pp. 31-45, 2020.
- [103] K.-J. Bathe, „Finite Element Method,” *Wiley Encyclopedia of Computer Science and Engineering*, 2008.
- [104] „<https://www.haascnc.com/machines/lathes/st/models/y-axis/st-15y.html>,” [Interactiv].
- [105] „<https://www.galdabini.eu/datasheets/quasar-25>,” [Interactiv].
- [106] „http://steelnumber.com/en/steel_composition_eu.php?name_id=8#1,” [Interactiv].
- [107] R. E. Petruse, S. Pușcașu, A. Pascu și I. Bondrea, „Key factors towards a high-quality additive manufacturing process with ABS material,” *Materialstoday: proceedings, Part of special issue: 35th Danubia Adria Symposium on Advances in Experimental Mechanics*, vol. 12, nr. 2, pp. 359-366, 2019.
- [108] T. D. Ngo, A. Kashani, G. Imbalzano, K. T. Q. Nguyen și D. Hui, „Additive manufacturing (3D printing): A review of materials, methods, applications and challenges,” *Composites Part B: Engineering*, vol. 143, pp. 172-196, 2018.
- [109] *ASTM F2792-12a*, ASTM International, 2015.
- [110] „<https://formlabs.com/eu/3d-printers/form-3/>,” [Interactiv].
- [111] E. F. Cicală, *Metode de prelucrare statica a datelor experimentale*, Timișoara: Editura Politehnica, 1999.